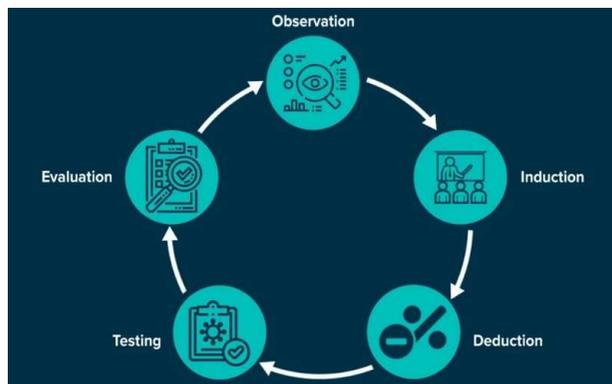


Empirical research in management and economics

Conjoint analysis

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Evaluation is now open

Please take part in the evaluation of the module!
Your feedback is highly appreciated.

Evaluation period: 10–23 January

Thanks!




Recap from last lecture

- What is the goal of cluster analysis, and how does it differ from factor analysis?
- Give two ways to measure similarity and describe how they differ from each other
- What's the purpose of linkage methods, and how do single linkage, complete linkage, and Ward's method differ from each other?
- Give a measure to quantify the model fit of a cluster solution
- Give two measures of model performance of a cluster solution that trade off model fit against model complexity
- What do high and low values on the Silhouette score mean?

Agenda for the semester

Session	Date	Topic
1	13 October	Introduction
2	20 October	Descriptive data analysis
3	27 October	Hypothesis development and measurement
4	3 November	Inferential data analysis I
5	10 November	Inferential data analysis II
6	17 November	Simple regression
7	24 November	Multiple regression
8	1 December	Logistic regression
9	8 December	Factor analysis
10	15 December	Cluster analysis
11	12 January	Conjoint analysis
12	19 January	The replication crisis and open science
13	26 January	Summary and questions
	11 February	Exam

Statistical software

- For the exercise, please download & install  and  Studio[®]
<https://www.rstudio.com/products/rstudio/download/#download>
- If you don't know R yet you can make yourself familiar with it
 - Free tutorials and help files
 - <http://www.r-tutor.com/r-introduction>
 - <https://cran.r-project.org/doc/contrib/Torfs+Brauer-Short-R-Intro.pdf>
 - You can take the free DataCamp online tutorial!
(<https://www.datacamp.com/courses/free-introduction-to-r>)



Goals for this week

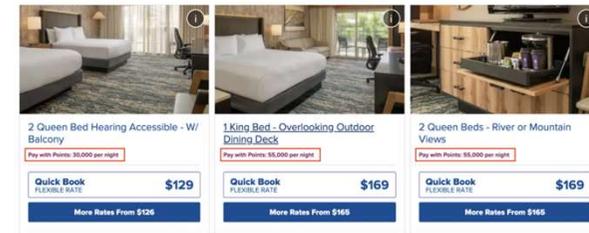
- You know the goals and principles of conjoint analysis
- You know how to design attribute profiles for collecting preference data for a conjoint analysis
- You are familiar with different methods for collecting preference data
- You know the general structure of a conjoint analysis model
- You understand what partworth utilities and attribute importances are and how they are calculated
- You understand how to use the results of a conjoint analysis to predict the utility of new attribute profiles

Decomposing people's preferences

- Marketing

What features of hotel rooms do guests care about?

→ Attributes: size of bed, size of room, type of view, balcony



- Education

What are the key aspects driving students' course preferences?

→ Attributes: applied content, quality of lecturer, credit requirements



- Medicine

What are key aspects for women's preferences between treatment options after a miscarriage?

→ Attributes: time in hospital, risk of complication, duration of recovery



Conjoint analysis



- Developed by Paul E. Green (e.g., Green & Rao, 1971; Green & Srinivasan, 1978)
- Basic assumption: Preference is based on a combination of all attributes (they are “CONsidered JOINTly“)
- Goal
 - Determine how important different attributes and attribute levels are for people’s preferences
 - It is a *decompositional* method
- Principle
 - Create options that represent combinations of different attribute levels and measure people’s preferences for the different options; then infer the impact of the different attributes and attribute levels on the preferences

Steps of a conjoint analysis



Selection of attributes and attribute levels

Automatic dosing mode	Price	Capacity	Power consumption
yes	600€	6kg	170 kWh/year
no	700€	8kg	140 kWh/year
	800€	10kg	110 kWh/year

Design of the options and collection of preferences

Washing machine B

- No automatic do
- Price: 600€
- Capacity: 8kg
- Power consumpt

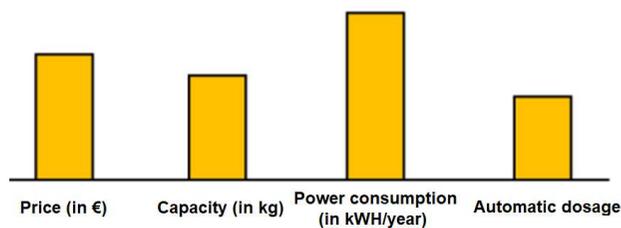
Washing machine A

- Automatic dosing
- Price: 700€
- Capacity: 8kg
- Power consumption: 140 kWh/year

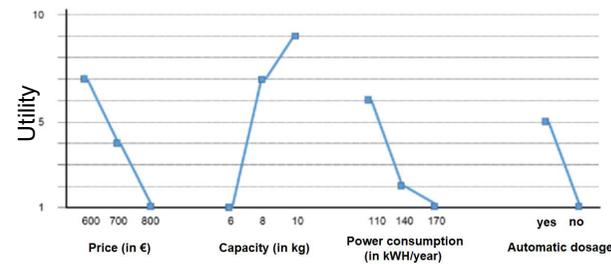
etc



Importance of the individual attributes



Partworth utilities



Criteria for selecting attributes and attribute levels

- *Relevance*: The attributes must be relevant for people's preferences
- *Actionable attributes*: The attributes should be modifiable
- *Realistic and feasible*: The attribute levels and their combinations have to be plausible
- *Manageable number of attributes and attribute levels*: The number of attributes and attribute levels should not be too high
- *Compensatoriness*: The attributes should be able to compensate for each other (e.g., an increase in price can be compensated by an improvement in taste). The attribute levels should not be exclusion criteria (e.g., a very high amount of calories cannot be compensated by a fancy packaging).
- *Independence*: The utility of an attribute level should not depend on the value of another attribute

A working example

Attributes

Attribute levels	Flavor	Price	Container	Topping
	Chocolate	1.50€	Cone	Yes
	Vanilla	2.00€	Cup	No
	Strawberry	2.50€		

$$L_{\text{Flavor}} = 3$$

$$L_{\text{Price}} = 3$$

$$L_{\text{Container}} = 2$$

$$L_{\text{Topping}} = 2$$

Ice cream!



Designing the options

Construction of the attribute profiles: Full factorial design

Attributes

Flavor	Price	Container	Topping
Chocolate	1.50€	Cone	Yes
Vanilla	2.00€	Cup	No
Strawberry	2.50€		

$L_{\text{Flavor}} = 3$ $L_{\text{Price}} = 3$ $L_{\text{Container}} = 2$ $L_{\text{Topping}} = 2$

→ $3 \times 3 \times 2 \times 2 = 36$ profiles

→ In a full factorial design, the attributes are orthogonal (i.e., uncorrelated)

Profile	Flavor	Price	Container	Topping	Profile	Flavor	Price	Container	Topping
1	Chocolate	1.50 EUR	Cone	Yes	19	Vanilla	2.00 EUR	Cup	Yes
2	Chocolate	1.50 EUR	Cone	No	20	Vanilla	2.00 EUR	Cup	No
3	Chocolate	1.50 EUR	Cup	Yes	21	Vanilla	2.50 EUR	Cone	Yes
4	Chocolate	1.50 EUR	Cup	No	22	Vanilla	2.50 EUR	Cone	No
5	Chocolate	2.00 EUR	Cone	Yes	23	Vanilla	2.50 EUR	Cup	Yes
6	Chocolate	2.00 EUR	Cone	No	24	Vanilla	2.50 EUR	Cup	No
7	Chocolate	2.00 EUR	Cup	Yes	25	Strawberry	1.50 EUR	Cone	Yes
8	Chocolate	2.00 EUR	Cup	No	26	Strawberry	1.50 EUR	Cone	No
9	Chocolate	2.50 EUR	Cone	Yes	27	Strawberry	1.50 EUR	Cup	Yes
10	Chocolate	2.50 EUR	Cone	No	28	Strawberry	1.50 EUR	Cup	No
11	Chocolate	2.50 EUR	Cup	Yes	29	Strawberry	2.00 EUR	Cone	Yes
12	Chocolate	2.50 EUR	Cup	No	30	Strawberry	2.00 EUR	Cone	No
13	Vanilla	1.50 EUR	Cone	Yes	31	Strawberry	2.00 EUR	Cup	Yes
14	Vanilla	1.50 EUR	Cone	No	32	Strawberry	2.00 EUR	Cup	No
15	Vanilla	1.50 EUR	Cup	Yes	33	Strawberry	2.50 EUR	Cone	Yes
16	Vanilla	1.50 EUR	Cup	No	34	Strawberry	2.50 EUR	Cone	No
17	Vanilla	2.00 EUR	Cone	Yes	35	Strawberry	2.50 EUR	Cup	Yes
18	Vanilla	2.00 EUR	Cone	No	36	Strawberry	2.50 EUR	Cup	No

Collecting preference data



Collecting preference data

Ordinal methods

- Ranking
 - “Please rank the 9 options according to how attractive you find them, that is, from most preferred (rank 1) to least preferred (rank 9).”
- Pair comparisons
 - “Please indicate which option you find more attractive.”
 - Option A vs. Option B
 - Option A vs. Option C
 - Option A vs. Option D
 - Option B vs. Option C
 - Option B vs. Option D
 - ...

Collecting preference data

Metric methods

- Rating scale
 - “Please indicate how attractive you find Option A on a scale from 1 (= not attractive at all) to 10 (= very attractive).“
- Dollar metric
 - “How much would you pay for Option A?“
 - “How much more would you pay for Option A relative to Option B?“
- Constant-sum method
 - “Distribute 100 points across the options such that a more strongly preferred option receives proportionally more points.“



	<i>Flavor</i>	<i>Price</i>	<i>Container</i>	<i>Topping</i>	Rank
Option 1	Vanilla	1.50 EUR	Cone	Yes	3
Option 2	Strawberry	2.00 EUR	Cone	Yes	4
Option 3	Chocolate	2.50 EUR	Cup	Yes	9
Option 4	Chocolate	1.50 EUR	Cone	No	8
Option 5	Chocolate	2.00 EUR	Cone	No	1
Option 6	Vanilla	2.50 EUR	Cone	No	5
Option 7	Strawberry	2.50 EUR	Cone	No	7
Option 8	Strawberry	1.50 EUR	Cup	No	6
Option 9	Vanilla	2.00 EUR	Cup	No	2



Ranking task



“Please rank the 9 options according to how attractive you find them—that is, from most preferred (rank 1) to least preferred (rank 9).”

Structure of a conjoint analysis model

Overall utility of object k

$$u_k = b_0 + \sum_{j=1}^J X_{jk} \times B_j$$

Intercept (base utility)

Coding matrix (representing the value of attribute j)

Regression coefficient matrix for attribute j

“Effect coding” of attribute values

For $L = 2$ attribute levels

	x_j
Level _{1,j}	1
Level _{2,j}	-1

× $[b_j]$

For $L = 3$ attribute levels

	$x_{j,1}$	$x_{j,2}$
Level _{1,j}	1	0
Level _{2,j}	0	1
Level _{3,j}	-1	-1

× $\begin{bmatrix} b_{j,1} \\ b_{j,2} \end{bmatrix}$

For $L = 4$ attribute levels

	$x_{j,1}$	$x_{j,2}$	$x_{j,3}$
Level _{1,j}	1	0	0
Level _{2,j}	0	1	0
Level _{3,j}	0	0	1
Level _{4,j}	-1	-1	-1

× $\begin{bmatrix} b_{j,1} \\ b_{j,2} \\ b_{j,3} \end{bmatrix}$

etc

Structure of a conjoint analysis model



Flavor	$x_{Flavor,1}$	$x_{Flavor,2}$
Chocolate	1	0
Vanilla	0	1
Strawberry	-1	-1

Price	$x_{Price,1}$	$x_{Price,2}$
1.50€	1	0
2.00€	0	1
2.50€	-1	-1

Container	$x_{Container}$
Cone	1
Cup	-1

Topping	$x_{Topping}$
Yes	1
No	-1

$$\begin{aligned}
 u_k = b_0 + & X_{Flavor,1} \times b_{Flavor,1} + X_{Flavor,2} \times b_{Flavor,2} + \\
 & X_{Price,1} \times b_{Price,1} + X_{Price,2} \times b_{Price,2} + \\
 & X_{Container} \times b_{Container} + \\
 & X_{Topping} \times b_{Topping}
 \end{aligned}$$



Structure of a conjoint analysis model

Flavor	$x_{\text{Flavor},1}$	$x_{\text{Flavor},2}$
Chocolate	1	0
Vanilla	0	1
Strawberry	-1	-1

Price	$x_{\text{Price},1}$	$x_{\text{Price},2}$
1.50€	1	0
2.00€	0	1
2.50€	-1	-1

Container	$x_{\text{Container}}$
Cone	1
Cup	-1

Topping	x_{Topping}
Yes	1
No	-1

$$\begin{aligned}
 u_k = & 4.75 + X_{\text{Flavor},1} \times -1 + X_{\text{Flavor},2} \times 1.667 + \\
 & X_{\text{Price},1} \times -0.667 + X_{\text{Price},2} \times 2.667 + \\
 & X_{\text{Container}} \times 0.5 + \\
 & X_{\text{Topping}} \times -0.25
 \end{aligned}$$

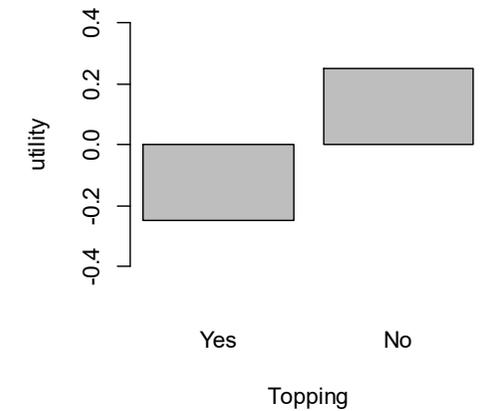
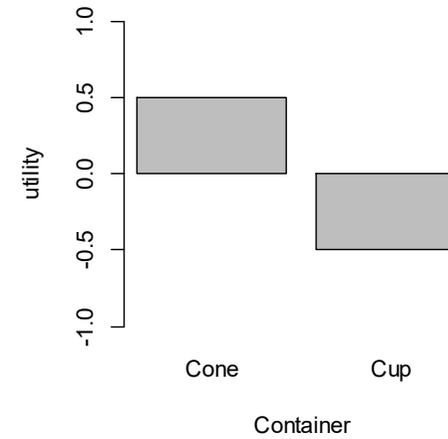
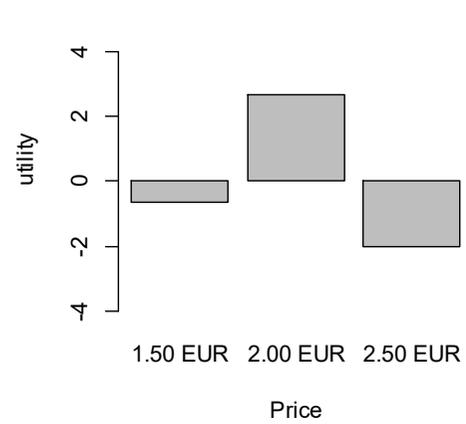
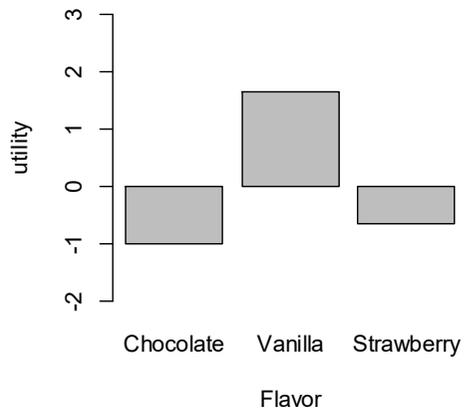
$$R^2 = .83$$

Partworth utilities



Attribute	Attribute levels	$x_{1,j}$	$x_{2,j}$	Regression weights (b)		Partworth utilities
				$b_{j,1}$	$b_{j,2}$	
Flavor	Chocolate	1	0			-1.000 $\leftarrow b_{Flavor,1} \times 1 + b_{Flavor,2} \times 0$
	Vanilla	0	1	-1.000	1.667	1.667 $\leftarrow b_{Flavor,1} \times 0 + b_{Flavor,2} \times 1$
	Strawberry	-1	-1			-0.667 $\leftarrow b_{Flavor,1} \times -1 + b_{Flavor,2} \times -1$
Price	1.50€	1	0			-0.667 $\leftarrow b_{Price,1} \times 1 + b_{Price,2} \times 0$
	2.00€	0	1	-0.667	2.667	2.667 $\leftarrow b_{Price,1} \times 0 + b_{Price,2} \times 1$
	2.50€	-1	-1			-2.000 $\leftarrow b_{Price,1} \times -1 + b_{Price,2} \times -1$
Container	Cone	1		0.500		0.500 $\leftarrow b_{Container} \times 1$
	Cup	-1				-0.500 $\leftarrow b_{Container} \times -1$
Topping	Yes	1				-0.250 $\leftarrow b_{Topping} \times 1$
	No	-1		-0.250		0.250 $\leftarrow b_{Topping} \times -1$

Partworth utilities



Attribute importance

Range of partworth utilities across attribute levels (l) for attribute j

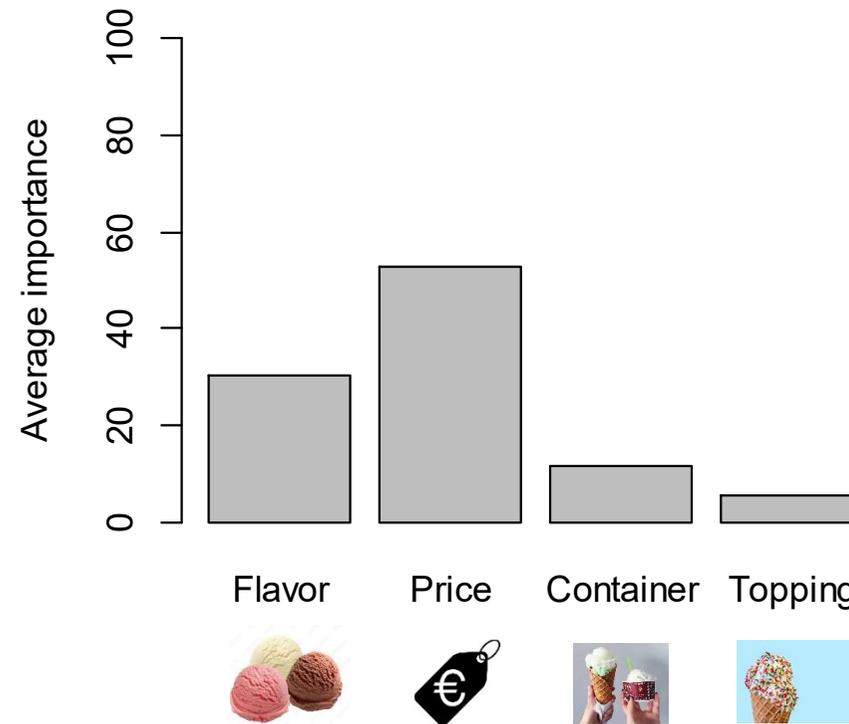
$$w_j = \frac{\max_l \{p_{jl}\} - \min_l \{p_{jl}\}}{\sum_{j=1}^J (\max_l \{p_{jl}\} - \min_l \{p_{jl}\})}$$

Attribute	Attribute levels	Partworth utilities (p)	Range	Importance (w)
Flavor	<i>Chocolate</i>	-1.000	1.667 - (-1.000) = 2.667	2.667/8.834 = 0.301
	<i>Vanilla</i>	1.667		
	<i>Strawberry</i>	-0.667		
Price	1.50€	-0.667	2.667 - (-2.000) = 4.667	4.667/8.834 = 0.529
	2.00€	2.667		
	2.50€	-2.000		
Container	<i>Cone</i>	0.500	0.500 - (-0.500) = 1.000	1.000/8.834 = 0.113
	<i>Cup</i>	-0.500		
Topping	<i>Yes</i>	-0.250	0.250 - (-0.250) = 0.500	0.500/8.834 = 0.057
	<i>No</i>	0.250		

$\Sigma = 8.834$

Attribute importance

$$w_j = \frac{\max_l \{p_{jl}\} - \min_l \{p_{jl}\}}{\sum_{j=1}^J (\max_l \{p_{jl}\} - \min_l \{p_{jl}\})}$$



Estimating the utility of the options

	Flavor	Price	Container	Topping
Option 1	Vanilla	1.50 EUR	Cone	Yes
Option 2	Strawberry	2.00 EUR	Cone	Yes
Option 3	Chocolate	2.50 EUR	Cup	Yes
Option 4	Chocolate	1.50 EUR	Cone	No
Option 5	Chocolate	2.00 EUR	Cone	No
Option 6	Vanilla	2.50 EUR	Cone	No
Option 7	Strawberry	2.50 EUR	Cone	No
Option 8	Strawberry	1.50 EUR	Cup	No
Option 9	Vanilla	2.00 EUR	Cup	No

Option 1

Flavor	Price	Container	Topping
Vanilla	1.50 EUR	Cone	Yes

Attribute	Attribute levels	$x_{1,j}$	$x_{2,j}$	$b_0 = 4.75$ Regression weights (b)		Partworth utilities
				$b_{j,1}$	$b_{j,2}$	
Flavor	Chocolate	1	0			-1.000
	Vanilla	0	1	-1.000	1.667	1.667
	Strawberry	-1	-1			-0.667
Price	1.50€	1	0			-0.667
	2.00€	0	1	-0.667	2.667	2.667
	2.50€	-1	-1			-2.000
Container	Cone	1		0.500		0.500
	Cup	-1				-0.500
Topping	Yes	1		-0.250		-0.250
	No	-1				0.250

$$u_k = b_0 + \sum_{j=1}^J X_{jk} \times B_j$$

$$u_{\text{Option 1}} = 4.75 + \underbrace{0 \times -1 + 1 \times 1.667}_{\text{Vanilla}} + \underbrace{1 \times -0.667 + 0 \times 2.667}_{1.50 \text{ EUR}} + \underbrace{1 \times .5}_{\text{Cone}} + \underbrace{1 \times -.25}_{\text{Topping}}$$

Partworth utility for:

➔ $u_{\text{Option 1}} = 6$



	<i>Flavor</i>	<i>Price</i>	<i>Container</i>	<i>Topping</i>	<i>Rank</i>	<i>u</i>
Option 1	Vanilla	1.50 EUR	Cone	Yes	3	6
Option 2	Strawberry	2.00 EUR	Cone	Yes	4	7
Option 3	Chocolate	2.50 EUR	Cup	Yes	9	1
Option 4	Chocolate	1.50 EUR	Cone	No	8	3.833
Option 5	Chocolate	2.00 EUR	Cone	No	1	7.167
Option 6	Vanilla	2.50 EUR	Cone	No	5	5.167
Option 7	Strawberry	2.50 EUR	Cone	No	7	2.833
Option 8	Strawberry	1.50 EUR	Cup	No	6	3.167
Option 9	Vanilla	2.00 EUR	Cup	No	2	8.833



Ranking task



“Please rank the 9 options according to how attractive you find them—that is, from most preferred (rank 1) to least preferred (rank 9).”

$$R^2 = .83$$

Using the results of a conjoint analysis

- **Revising an existing product portfolio**
 - Which products (and attribute levels) could be eliminated from the product portfolio?
 - How sensitive would customers be to changes in an attribute (e.g., an increase in price)?
- **Simulating customer preferences for new products**
 - Which new combination of attribute levels should be introduced?

Predicting the utility of a new profile

Flavor	Price	Container	Topping
Strawberry	2.00 EUR	Cone	No

Attribute	Attribute levels	$x_{1,j}$	$x_{2,j}$	$b_0 = 4.75$ Regression weights (b)		Partworth utilities
				$b_{j,1}$	$b_{j,2}$	
Flavor	Chocolate	1	0			-1.000
	Vanilla	0	1	-1.000	1.667	1.667
	Strawberry	-1	-1			-0.667
Price	1.50€	1	0			-0.667
	2.00€	0	1	-0.667	2.667	2.667
	2.50€	-1	-1			-2.000
Container	Cone	1		0.500		0.500
	Cup	-1				-0.500
Topping	Yes	1				-0.250
	No	-1		-0.250		0.250

$$u_k = b_0 + \sum_{j=1}^J X_{jk} \times B_j$$

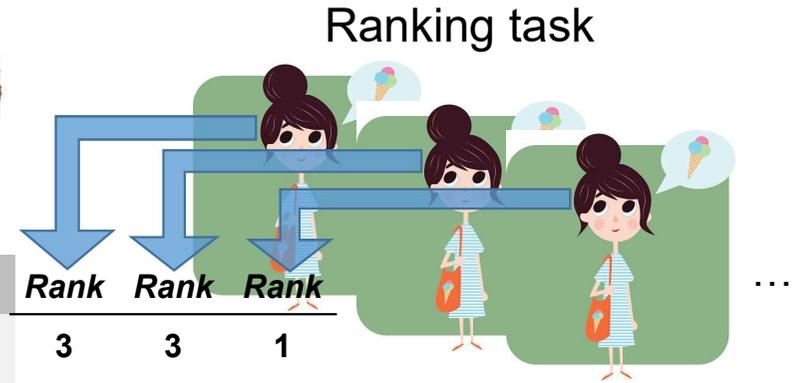
$$u_{new} = 4.75 - 1 \times -1 + -1 \times 1.667 + 0 \times -0.667 + 1 \times 2.667 + 1 \times .5 + -1 \times -.25$$

Partworth utility for: Strawberry 2.00 EUR Cone No topping

➔ $u_{new} = 7.5$



	<i>Flavor</i>	<i>Price</i>	<i>Container</i>	<i>Topping</i>
Option 1	Vanilla	1.50 EUR	Cone	Yes
Option 2	Strawberry	2.00 EUR	Cone	Yes
Option 3	Chocolate	2.50 EUR	Cup	Yes
Option 4	Chocolate	1.50 EUR	Cone	No
Option 5	Chocolate	2.00 EUR	Cone	No
Option 6	Vanilla	2.50 EUR	Cone	No
Option 7	Strawberry	2.50 EUR	Cone	No
Option 8	Strawberry	1.50 EUR	Cup	No
Option 9	Vanilla	2.00 EUR	Cup	No



“Please rank the 9 options according to how attractive you find them, that is from most preferred (rank 1) to least preferred (rank 9).”

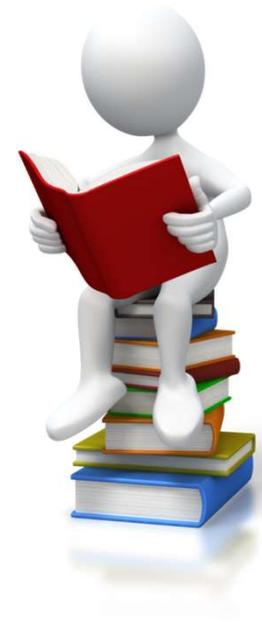
Self-quiz questions

- What is the goal of conjoint analysis?
- What are important criteria when designing attribute profiles for a conjoint analysis?
- How does a fractional orthogonal design differ from a full factorial design? What does it mean if a fractional design is orthogonal?
- Give different approaches to collect preference data
- What is the structure of a conjoint analysis model?
- How does effect coding differ from dummy coding?
- Describe the calculation of partworth utilities
- Describe the calculation of attribute importances

Background reading for next week

Pennington, C. R. (2023). A student's guide to open science. In: C. R. Pennington, *A student's guide to open science. Using the replication crisis to reform psychology* (p. 56–75). McGraw Hill, Open University Press.

Andraszewicz, S., Scheibehenne, B., Rieskamp, J., Grasman, R., Verhagen, J., & Wagenmakers, E. J. (2015). An introduction to Bayesian hypothesis testing for management research. *Journal of Management*, 41(2), 521–543.



Homework for Exercise next week

Watch this brief tutorial (< 9 min) on preparing a preregistration on  AS PREDICTED

https://www.youtube.com/watch?v=7ic_BgpmakI

